

Theory

ADF Program System

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INTRODUCTION

This document discusses theoretical aspects related to the ADF program package, directed at special applications that may require more attention than is worked out in the User's Guide, which focuses on defining input keys and elementary control of the calculations.

With the other documentation to the ADF package, this document is available on-line at <http://www.scm.com>

1 MULTIPLET ENERGIES

The energies of atomic and molecular multiplet states that correspond to a given electron configuration can be calculated approximately with the method suggested in ref. [1]. There it is indicated that it would not be justified to take an arbitrary configuration-state function (CSF), defined in general as a linear combination of determinants that has specific spin and space symmetry properties, and use the corresponding α and β spin densities in a DFT energy expression. The same holds true for the densities corresponding to the average-of-configuration (see section 1.1, the “procedure” notes).

Therefore, we restrict ourselves to just computing the DFT energies of single-determinant wavefunctions. Usually (but not always) this is sufficient information to obtain the multiplet energies. The procedure, which is explained in [1], requires knowledge of the CSFs belonging to a given configuration. This means that a multiplet state with specific L, M_L and S, M_S values has to be written as a linear combination of the determinant wavefunctions that belong to the given configuration. With the auxiliary program ASF (A d Single-determinants Eribourg, developed by Claude Daul in Fribourg, Switzerland) all the CSFs can be obtained, printed as linear combinations of the determinants [2]. The inverse transformation yields the determinants written as linear combinations of the CSFs.

It is often advantageous to search for CSFs that consist of one determinant only, since the energy of this determinant should correspond directly to the multiplet energy. Sometimes there is redundancy in the information and there may even be some inconsistency: two determinants may exist that both are CSFs belonging to the same multiplet state but yield somewhat different energies. We will illustrate this for the Carbon atom example treated below.

The discrepancies are a measure of ‘error bars’ associated with the theoretical multiplet energies. As a matter of fact, there are certain symmetry relations between the energies of the determinants of a configuration, calculated as the expectation value of the determinant for the full many-electron Hamiltonian. An example is the equal energy for the determinants of a p^1 configuration, whether the electron is placed in the $p_0 (=p_z)$ orbital or in the $p_{+1} (= (p_x + ip_y)/\sqrt{2})$ orbital. This equality is not obtained with present-day density functionals, leaving an ambiguity (‘error bar’) in the determination of the energy. A more complete treatment of the symmetry relations between determinant energies is given in [2].

The auxiliary program ASF, that for finite point groups finds the CSFs as linear combinations of determinants, performs also a symmetry analysis of all the two-electron integrals for a configuration, reducing them to a minimum number of non-redundant ones. ASF expresses the energies of the multiplets in the non-redundant two-electron integrals. However (WARNING!), there have occasionally been found inconsistent results. A comparison to the results obtained by the procedure outlined in [1] may show significant differences and the latter seem more accurate and consistent.

1.1 DFT ENERGY OF A ONE-DETERMINANTAL WAVEFUNCTION

The determinant corresponds to a well defined ρ^α and ρ^β . Suppose we are dealing with a d^2 configuration and we wish to know the energy of

$$D_1 = |d_2^\alpha(1)d_1^\alpha(2)|$$

where d_m has the Y_{2m} angular part. This determinant is a CSF of the 3F multiplet:

$$D_1 = |{}^3F; M_L = 3, M_S = 1|$$

We can easily transform to the real spherical harmonics that are used in ADF:

$$Z_{lm}^c = \frac{1}{\sqrt{2}}(Y_l^{-m} + Y_l^{-m*}) = \frac{1}{\sqrt{2}}(Y_l^{-m} + (-1)^m Y_l^m)$$

$$Z_{lm}^s = \frac{i}{\sqrt{2}}(Y_l^{-m} + Y_l^{-m*}) = \frac{i}{\sqrt{2}}(Y_l^{-m} + (-1)^m Y_l^m)$$

with back transformations:

$$Y_l^m = \frac{1}{\sqrt{2}}(-1)^m Z_{lm}^c + \frac{i}{\sqrt{2}}(-1)^m Z_{lm}^s$$

$$Y_l^{-m} = \frac{1}{\sqrt{2}} Z_{lm}^c - \frac{i}{\sqrt{2}} Z_{lm}^s$$

Here the superscripts c and s stand for the cosine, respectively sine type of combinations of $\exp(-im\phi)$ and $\exp(im\phi)$. This yields explicitly:

$$d_{z^2} = d_0$$

$$d_0 = d_{z^2}$$

$$d_{xz} = \frac{1}{\sqrt{2}}(d_{-1} - d_1)$$

$$d_1 = -\frac{1}{\sqrt{2}}d_{xz} - \frac{i}{\sqrt{2}}d_{yz}$$

$$d_{yz} = \frac{i}{\sqrt{2}}(d_{-1} + d_1)$$

$$d_{-1} = \sqrt{2}\frac{1}{\sqrt{2}}d_{xz} - \frac{i}{\sqrt{2}}d_{yz}$$

$$d_{x^2-y^2} = \frac{1}{\sqrt{2}}(d_{-2} + d_2)$$

$$d_2 = \frac{1}{\sqrt{2}}d_{x^2-y^2} + \frac{i}{\sqrt{2}}d_{xy}$$

$$d_{xy} = \frac{i}{\sqrt{2}}(d_{-2} - d_2) \qquad d_{-2} = \frac{1}{\sqrt{2}}d_{x^2-y^2} - \frac{i}{\sqrt{2}}d_{xy}$$

For D_1 we obtain:

$$\rho^\alpha = |d_2|^2 + |d_1|^2 = \frac{1}{2}|d_{x^2-y^2}|^2 + \frac{1}{2}|d_{xy}|^2 + \frac{1}{2}|d_{xz}|^2 + \frac{1}{2}|d_{yz}|^2$$

$$\rho^\beta = 0$$

The fractional occupations have to be used in order to generate the densities ρ^α and ρ^β and the corresponding density matrices P^α and P^β . The density matrices can be used to calculate the energy of D_1 (and 3F) with respect to the energy of the 'master fragment', which should be the restricted atom with d^2 occupation. Other determinants of this configuration can be treated similarly to obtain more multiplet energies of the d^2 configuration.

Below is an example of how you can obtain determinant energies 'by hand', i.e. by carrying out a specific sequence of ADF calculations. ADF supports an automatic procedure to do this, using the input key `SLATERDETERMINANTS`, see the ADF User's Guide, the Examples document, and below.

Procedure

1° Determine a set of orbitals belonging to the given configuration. These orbitals are generated in what we call the average-of-configuration (AOC) calculation. This is a spin-restricted SCF calculation where the electrons of the configuration are distributed equally over the subspecies of the open shell irreps in order to retain the A_1 symmetry of the total density in the symmetry group of the molecule. For instance, in case of an atomic d^2 configuration, the AOC calculation can be done in symmetry `ATOM` with occupation 2 in the `d` irrep. In case of an $t_{2g}^5 e_g^1$ configuration of an octahedral complex, the AOC calculation requires an occupation of 5 electrons in the `t2g`, and 1 electron in the `eg`.

The result file `TAPE21` of the AOC calculation has to be saved, to be used as a fragment file in the subsequent calculations.

2° The AOC is used as a fragment in all subsequent calculations that are performed to obtain single determinant energies. This means that those single determinant energies are always with respect to the AOC energy. This is a case where there is only one "fragment", which is actually the complete system, but in a different electronic configuration and in possibly a different symmetry group.

Suppose that a single determinant corresponds to spin-up and spin-down densities ρ^α and ρ^β , i.e. to specific spin-unrestricted occupations of the AOC orbitals. These densities ρ^α and ρ^β correspond to a symmetry group that will in general be a subgroup of the symmetry group of the molecule. For instance, the occupation $(p_{+1}\alpha)^1$ in the case of an atomic p^1 configuration corresponds to

$$\rho^\alpha = \frac{1}{2}p_x^2 + \frac{1}{2}p_y^2$$

with $D_{\infty h}$ symmetry.

To obtain the energy of the determinant wavefunction we must now perform *one* cycle (*ITERATIONS*= 0 in the block key *SCF*) of a spin-unrestricted calculation, with AOC as (the only) fragment with α and β occupation numbers (using the input key *OCCUPATIONS*) such that ρ^α and ρ^β result. Note that the appropriate (lower) symmetry pointgroup must be specified in the input file.

Occasionally, the single determinant corresponds to a closed shell configuration in the appropriate lower symmetry, for instance determinant $D_{10} = |0^+ 0^-|$ of the p^2 configuration of Carbon, with density $\rho=p_z^2$. In that case the one-cycle calculation can of course be spin-restricted.

N.B.1. One cycle will regenerate the SCF orbitals of AOC, if the same field is used as the converged AOC field. This will actually be the case because the starting potential is taken from the fragment TAPE21 file.

The key *MODIFYSTARTPOTENTIAL* must not be used (the density should be distributed equally over the spins).

N.B.2. After diagonalization in the one-cycle run, the AOC orbitals have been obtained again and are occupied as specified. The ('bonding') energy is calculated from the resulting charge density.

Remarks:

- If one does not perform just one cycle, but instead converges the unrestricted calculation, the energy will be lowered by 'polarization' of the orbitals. It is theoretically not so clear what the status of such converged energies is. Usually the energy lowering is in the order of 0.1 eV, but it may be quite a bit larger.
- It is not necessary to use AOC as fragment in the single-determinant runs. It is also perfectly allowed to run all calculations (ground state, AOC, determinants) from one set of fragments, for instance the standard atomic fragments. Since we must arrange that the one-cycle determinant calculations use the AOC field, so as to reproduce the AOC orbitals, we must then supply the result file TAPE21 of the AOC run as a restart file, using the key *RESTART*; see the ADF User's Guide.

Of course, in such an approach the computed energies are with respect to another reference, for instance the restricted atoms.

Results for first and second period atoms

In the appendix tables are given for the energy lowering in going from the converged spherically symmetric spin-restricted atom (the 'master' fragment) to specific one-determinant wavefunctions with the orbital occupations as specified. Note that the p_x and p_y populations are always equal; only their sum is given. In many cases the determinant corresponds to a specific state, which is then given in the last column. For each atom, the first calculation is for the spherically symmetric spin-*un*restricted atom. These tables are now obsolete, all information needed to obtain the atomic reference energies, i.e. the groundstate multiplet energy with respect to the AOC, can be found in ref. [3].

Examples worked out for all first and second period atoms:

H: Configuration $(1s)^1$.
Only one determinant: $|1s\alpha(1)|$

Li: Configuration $(2s)^1$.
Only one determinant: $|2s\alpha(1)|$

Be: Configuration $(2s)^2$.
Closed shell.

B: Configuration $(2p)^1$.
Ground multiplet 2P .

$$D_1 = |p_1\alpha(1)| = \left| ^2P; M_L = 1, M_S = \frac{1}{2} \right\rangle$$

$$\rho^\alpha = |p_1| = \left(-\frac{1}{\sqrt{2}}p_x - \frac{i}{\sqrt{2}}p_y \right)^* \left(-\frac{1}{\sqrt{2}}p_x - \frac{i}{\sqrt{2}}p_y \right)$$

$$\rho^\alpha = \frac{1}{2}(p_x - ip_y)(p_x + ip_y) = \frac{1}{2}(p_x^2 + p_y^2)$$

The occupation numbers for D_1 are

$$p_x^\alpha = p_y^\alpha = \frac{1}{2}; p_z^\alpha = 0; p_x^\beta = p_y^\beta = p_z^\beta = 0$$

Another determinant belonging to 2P is

$$D_2 = |..p_0\alpha(1)|$$

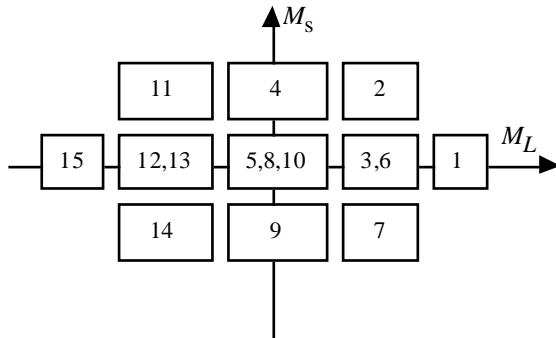
with occupations $p_z^\alpha = 1$ and all other p-occupations zero. This determinant is ~ 0.04 eV lower in energy than D_1 for vWN, but ~ 0.15 eV for vWN + Becke's GGA exchange correction.

C: Configuration p^2 .
Multiplet states are 3P , 1S and 1D .

We use this atom as an example of the general procedure. First write down all determinants belonging to p^2 and group them according to M_S and M_L

$$(1^+ \equiv p_1\alpha, \dots)$$

<u>Determinant</u>	<u>MS</u>	<u>ML</u>
$D_1 = 1^+ 1^- $	0	2
$D_2 = 1^+ 0^+ $	1	1
$D_3 = 1^+ 0^- $	0	1
$D_4 = 1^+ -1^+ $	1	0
$D_5 = 1^+ -1^- $	0	0
$D_6 = 1^- 0^+ $	0	1
$D_7 = 1^- 0^- $	-1	1
$D_8 = 1^- -1^+ $	0	0
$D_9 = 1^- -1^- $	-1	0
$D_{10} = 0^+ 0^- $	0	0
$D_{11} = 0^+ -1^+ $	1	-1
$D_{12} = 0^+ -1^- $	0	-1
$D_{13} = 0^- -1^+ $	0	-1
$D_{14} = 0^- -1^- $	-1	-1
$D_{15} = -1^+ -1^- $	0	-2



The presence of a determinant with $M_L = 2$, $M_S = 0$ and no $M_L = 2$, $M_S > 0$ determinant indicates the presence of a 1D multiplet, and $E(^1D) = E(D_1)$.

There is also a 3P , the determinant with $M_S = 1$, $M_L = 1$. We should have $E(^3P) = E(D_2) = E(D_4)$. The two determinants D_3 and D_6 in the $M_S = 0$, $M_L = 1$ box will mix, and the solutions of the 2 by 2 secular problem will be $E(^1D)$ and $E(^3P)$. Since the sum of the eigenvalues is equal to the sum of the initial diagonal elements, we have $E(^1D) + E(^3P) = E(D_3) + E(D_6)$.

We should also have $E(D_3) + E(D_6) = E(D_1) + E(D_2)$. Such a relation provides a test on the consistency of the results.

Finally we have the $M_S = 0$, $M_L = 0$ block. The sum of the energies of D_5 , D_8 and D_{10} should be the sum of the energies of 1S , 3P and 1D . Since $E(^3P)$ and $E(^1D)$ are already known, $E(^1S)$ can be calculated.

In the appendix we first locate for C the spherical unrestricted atom. Next we have $E(D_4)$, yielding $E(^3P) = -1.345$ eV (vWN + Becke). Next $E(D_2) = E(^3P) = -1.189$ (always vWN + Becke). The difference is substantial: ~ 0.15

Next we have $E(D_3) = -0.812$. Since $E(D_6) = E(D_3)$, because $\rho^\alpha(D_6) = \rho^\beta(D_3)$ and $\rho^\beta(D_6) = \rho^\alpha(D_3)$, we should have $2E(D_3) = -1.624 = E(^1D) + E(^3P)$. Therefore $E(^1D) = -1.624 - (-1.345) = -0.279$ or $E(^1D) = -1.624 - (-1.189) = -0.435$.

These numbers can be checked against $E(D_1)$ which also should be $E(^1D)$:

$E(D_1) = +0.044$. The discrepancy is large!

Finally, 1S can be obtained:

$$E(D_{10}) = +0.319$$

$$(D_8) = E(D_1) = +0.044$$

$$E(D_5) = E(D_1) = +0.044$$

$$\text{So } 0.407 = E(^1S) + E(^3P) + E(^1D).$$

Different results for $E(^1S)$ are obtained depending on the $E(^3P)$ and $E(^1D)$ we choose:

$$\text{e.g. } E(^1S) = 0.407 - (-1.345) - (-0.279) = 2.031$$

$$\text{or } E(^1S) = 0.407 - (-1.189) - (0.044) = 1.552.$$

Comparing to experiment we might calculate the excitation energies w.r.t. $E(^3P)$:

	calculated	experimental	HF
$^3P \rightarrow ^1D$:	1.066 to 1.389	1.26	1.55
$^3P \rightarrow ^1S$:	2.741 to 3.376	2.684	3.78

N:

Configuration p^3 .

Ground multiplet 4S , corresponds to the spherical unrestricted atom, energy -2.943 eV. Other multiplets: 2P , 2D . According to the printed output for configuration p^3 we have

$$\left| ^2D; M_L = 2, M_S = \frac{1}{2} \right\rangle = |p_1^\alpha p_1^\beta p_0^\alpha| = D_2$$

$$\rho^\alpha = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2 + p_z^2$$

$$\rho^\beta = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2$$

$E(D_2) = -0.745$ according to the table in the Appendix (VWN + Becke)

The energy of D_1 , with $\rho^\alpha = p_x^2 + p_y^2, \rho^\beta = p_z^2$, is $E(|1A 2B 3A|) = -1.9702$.

The energy of D_3 , with $\rho^\alpha = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2 + p_z^2, \rho^\beta = p_z^2$ corresponding to $|1A 2A 2B|$ or $|2A 2B 3A|$, is $E(D_3) = -0.158$.

Finally, D_4 has $\rho^\alpha = p_x^2 + p_y^2, \rho^\beta = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2$, corresponding to $|1A 1B 3A|$ and $|1A 3A 3B|$, and $E(D_4) = -0.109$.

The $M_L = 1, M_S = \frac{1}{2}$ determinants are $|1A 1B 3A|$ and $|1A 2A 2B|$. Therefore $E(^2D) + E(^2P) = E(D_4) + E(D_3)$, so $E(^2P) = -0.109 - 0.158 - (-0.745) = +0.478$.

We can use D_1 in the $M_L = 0, M_S = \frac{1}{2}$ block, from which we find $E(^4S) + E(^2D) + E(^2P) = 2E(D_2) = +E(D_1)$.

Hence $E(^2P) = -1.490 - 1.9702 - (-0.745) - (-2.943) = +0.2278$.

O:

Configuration p^4 .

Multiplet states 3P , 1S , 1D .

D_1 , with $\rho^\alpha = p_x^2 + p_y^2 + p_z^2, \rho^\beta = p_z^2$ corresponds to $|1A 2A 2B 3A|$, the $M_L = 0, M_S = 1$ determinant of 3P : $E(^3P) = -1.836$

D_2 with $\rho^\alpha = p_x^2 + p_y^2 + p_z^2, \rho^\beta = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2$, corresponds to $|1A 1B 2A 3A|$, the $M_L = 1, M_S = 1$ determinant of 3P : $E(^3P) = -1.568$

D_3 , with $\rho^\alpha = \frac{1}{2} p_x^2 + \frac{1}{2} p_y^2 + p_z^2, \rho^\beta = p_x^2 + p_y^2$, corresponds to $|1A 1B 2A 3B|$, $M_L = 1, M_S = 0$ and belonging to 3P as well as 1D .

F:

Configuration p^5 .

Ground multiplet 2P .

As in B, we have two determinants with different energies belonging to this state:

$$D_1 = \left| \dots (p_0^\alpha)^1 (p_0^\beta)^0 \right| \rightarrow E(D_1) = -0.715.$$

$$D_2 = \left| (p_{-1})^2 (p_0)^2 (p_1^\alpha)^1 (p_1^\beta)^0 \right| \rightarrow E(D_2) = -0.467.$$

1.2 GROUND AND EXCITED STATE MULTIPLETS

The computation of multiplets can be carried out with ADF, using the input key `SLATERDETERMINANTS`. The method described in [1] for the calculation of the energies of proper spin and spatial symmetry adapted Configuration State Functions is based on the calculation of the energies of single determinantal wavefunctions. The densities corresponding to those Slater determinants are inserted in the approximation used for the exchange-correlation energy.

The procedure as detailed above is somewhat involved. Moreover, one would like to have an easy procedure to calculate many determinants. This is particularly desirable if one wishes to calculate the energies of all Slater determinants of a given configuration, for instance if one wishes to calculate certain averages in view of the inconsistencies of the method.

We have implemented a semi-automatic procedure, using the key `SLATERDETERMINANTS`.

The general idea of this method is to first perform a restricted calculation in the symmetry that is appropriate for the molecule. This is called the average-of-configuration (AOC) calculation. This AOC calculation generates the orbitals which will be used in all the Slater determinants.

The AOC is the fragment that *must* be used in all subsequent calculations. The subsequent calculations are characterized by having the AOC as the (only) fragment, and by specifying the keyword `SLATERDETERMINANTS`. This key is a general key: it may be used as a simple key (it must then have an argument) or as a block type key (no argument, but a data block). If an argument is given this must be a file name. The named file should contain the occupations for the determinants (see below). If no file name is specified the key should be a block key and the occupations should be specified in the data block.

The required information, on file or in the data block, is the specification of the determinant or determinants that are to be calculated in the form of orbital occupation numbers for the AOC orbitals, using the irrep labels of the point group of the AOC calculation, see below for format. All specified determinants will be calculated, and the obtained energy will always be the energy difference with respect to the AOC. Default occupations for all subspecies of the AOC fragment are the occupations of the AOC itself. Therefore, only the open (modified) subspecies have to be specified.

One has to be careful with respect to the point group symmetry to use in the `SLATERDETERMINANTS` calculation. The density belonging to a specific determinant is usually lower than the AOC symmetry (which is the full symmetry group of the system). In that case this lower point group symmetry has to be specified in the `SLATERDETERMINANTS` calculation. Everything will always work fine if one just does not use any symmetry at all (`NOSYM`). However, if for reasons of computational efficiency one does want to use a subgroup of the system that corresponds to the determinant density or densities, this is perfectly possible. However, all the densities of the determinants specified *must* then have this (or a higher) symmetry. The program does not check on this, it is the user's responsibility to make sure that this condition is satisfied for all the determinants. The only check that is performed is that occupations of equivalent representations (subspecies of one irrep) in the lower point group of the `SLATERDETERMINANTS` run, that result from the specified occupations of the subspecies of the AOC symmetry, are equal.

Format of the input.

Important: in the SlaterDeterminants calculations it is imperative that the results are obtained in the AOC field: no SCF convergence must be carried out, because we only want to assign the electrons differently, while keeping

the AOC orbitals exactly as they are. To achieve this, the calculations should use the keyword `SCF`, and the subkey `ITERATIONS` has to be set to 0 in the `SCF` data block.

Since ADF requires that the point-group symmetry conforms not only to the nuclear frame but also to the electronic charge density and MO occupations, these calculations must run in a lower pointgroup symmetry. Often you will also want to run the modified calculations spin-*unrestricted*. For an example, see the set of sample runs that come with the package and the comments in the Examples document.

The calculation of the one-determinant states based on the AOC reference state is controlled with the key `SLATERDETERMINANTS`. It is a *general* key; it can be used as a simple key and requires an argument then. It can also be used as a block key. For this particular key it is not correct to specify an argument *and* a data block.

```
| SLATERDETERMINANTS  file
```

When used as a simple key, the argument must be a file (including the path). The file must be an ASCII file containing data in the same format as you would supply in the data block when using the key as block type key, see below. All information on the file until the *eof* must be suitable for the data block, but no record 'end' on the file must be specified: only the *contents* of the data block.

The block format:

```
| SLATERDETERMINANTS
| TITLE1
|     irrep  occupies
|     irrep  occupies
|     ....
| SUBEND
| TITLE2
|     irrep  occupies
|     .....
| SUBEND
| TITLE3
|     ....
| SUBEND
|     ....
| END
```

Each "`TITLE`" functions as a subkey, but is otherwise an arbitrary string to label the resulting one-determinant calculation. Each such subkey block contains the occupation numbers for a single one-determinant calculation. It is necessary that the calculation uses the reference AOC run as its only fragment file. The occupations in the subkey blocks must be re-arrangements of the AOC open-shell electrons. In the `SLATERDETERMINANTS` calculation you must explicitly specify the pointgroup symmetry in which you want to run. The ρ^α and

ρ^β densities of all determinants to be calculated must have this point group symmetry, or a higher symmetry.

Each “irrep occupies” record specifies the occupations for the indicated irrep in the usual way (see for instance the OCCUPATIONS key). The irrep labels must correspond to the AOC point group symmetry used in the AOC calculation, *not the point group symmetry used in the SLATERDETERMINANTS calculation!*. Note that in an unrestricted calculations, occupations numbers must be given for both spins, using the double slash (//) to separate the occupations for spin-alpha and spin-beta.

In this setup, the program will for each of the subkey blocks under the SLATERDETERMINANTS key execute an SCF calculation with only one cycle, i.e. no convergence, where the start-up field is the fragment field, i.e. the AOC field. So all one-determinant states in this calculation are evaluated in the AOC field. The resulting energies for the distinctly computed one-determinant states can then be combined to the desired multiplet values.

Example: Carbon p^2

```
SlaterDeterminants
C(p2) ALFA: s=1, px=py=4/3, pz=2/3; BETA: s=1, p=0 ! title
  S      1 // 1 ! irrep name and occupations
  P:x    0.6666666666666666 // 0 ! another irrep, et cetera
  P:y    0.6666666666666666 // 0
  P:z    0.6666666666666666 // 0
  D:z2   0 // 0
  D:x2-y2 0 // 0
  D:xy   0 // 0
  D:xz   0 // 0
  D:yz   0 // 0
SUBEND
C(p2) ALFA: S=1, px=py=1, pz=0; BETA: s=1 !next (Sl.Determinant) title
  S      1 // 1
  P:x    1 // 0
  P:y    1 // 0
  P:z    0 // 0
  D:z2   0 // 0
  D:x2-y2 0 // 0
  D:xy   0 // 0
  D:xz   0 // 0
  D:yz   0 // 0
SUBEND
C(p2) ALFA: s=1, px=py=0.5, pz=1; BETA: s=1
  S      1 // 1
  P:x    0.5 // 0
  P:y    0.5 // 0
  P:z    1 // 0
  D:z2   0 // 0
  D:x2-y2 0 // 0
  D:xy   0 // 0
  D:xz   0 // 0
  D:yz   0 // 0
SUBEND
```

```

C(p2) ALFA: s=1, px=py=0.5, pz=0; BETA: s=1, px=py=0, pz=1
S      1 // 1
P:x    0.5 // 0
P:y    0.5 // 0
P:z    0 // 1
D:z2   0 // 0
D:x2-y2 0 // 0
D:xy   0 // 0
D:xz   0 // 0
D:yz   0 // 0
SUBEND
C(p2) ALFA: s=1, px=py=0.5, pz=0; BETA: s=1, px=py=0.5, pz=0
S      1 // 1
P:x    0.5 // 0.5
P:y    0.5 // 0.5
P:z    0 // 0
D:z2   0 // 0
D:x2-y2 0 // 0
D:xy   0 // 0
D:xz   0 // 0
D:yz   0 // 0
SUBEND
C(p2) ALFA: s= 1, px=py=0, pz=1; BETA: s=1, px=py=0, pz=1
S      1 // 1
P:x    0 // 0
P:y    0 // 0
P:z    1 // 1
D:z2   0 // 0
D:x2-y2 0 // 0
D:xy   0 // 0
D:xz   0 // 0
D:yz   0 // 0
SUBEND

```

In the example the AOC calculation is the Carbon atom in spherical symmetry (symmetry name ATOM). Several spin states can be generated from this AOC set of orbitals, but they all have a lower symmetry than the AOC. In the example the point group $D_{\infty h}$ (DLIN) could be used in the SLATERDETERMINANTS calculation. In $D_{\infty h}$ the p orbitals split into two sets, p_x and p_y occur in π_x and π_y respectively, so their occupations must be identical, and p_z is a Σ_u orbital.

In the data block of the SLATERDETERMINANTS key (or in the file) we now specify the occupations for the subspecies of the ATOM irreps of a specific Slater determinant and the program will sort out the corresponding occupations in the D(LIN) symmetry.

In all cases the orbitals used for the energy calculation(s) will be the self-consistent AOC orbitals.

In the given example, the first set of occupations does not correspond to a Slater determinant, but is the spin-polarized spherical case with the p electrons evenly distributed over all components.

1.3 APPENDIX

X α ($\alpha = 0.7$) results, with and without GGA (Becke-Perdew)

Energy changes (eV) for atoms, when going from restricted to (one-cycle) unrestricted. Results between parentheses are for *converged* unrestricted calculations.

All calculations have been performed in $D_{\infty h}$ symmetry, since p_x and p_y always had equal occupations and therefore could occur as π_u -x and π_u -y partners of the Γ_u irrep.

El.	Occupations						X α	X α +Becke	X α +Becke +Perdew
	α -spin			β -spin					
	s	p_x+p_y	p_z	s	p_x+p_y	p_z			
H	1	0	0	0	0	0	-1.414 (-1.465)	-1.305 (-1.420)	-1.434 (-1.525)
Li	1	0	0	0	0	0	-0.520 (-0.531)	-0.484 (-0.507)	-0.536 (-0.551)
Be	1	0	0	1	0	0	0.000 (0.000)	0.000 (0.000)	0.000 (0.000)
B	1	2/3	1/3	1	0	0	-0.373 (-0.382)	-0.356 (-0.370)	-0.402 (-0.408)
	1	0	1	1	0	0	-0.471 (-0.521)	-0.608 (-0.680)	-0.622 (-0.693)
C	1	1	0	1	0	0	-0.406 (-0.427)	-0.435 (-0.466)	-0.472 (-0.498)
	1	4/3	2/3	1	0	0	-1.634 (-1.686)	-1.580 (-1.643)	-1.723 (-1.768)
	1	2	0	1	0	0	-1.670 (-1.759)	-1.787 (-1.900)	-1.889 (-1.990)
	1	1	1	1	0	0	-1.634 (-1.694)	-1.615 (-1.689)	-1.748 (-1.805)
	1	1	0	1	0	1	-0.664 (-0.750)	-0.925 (-1.071)	-0.977 (-1.131)
N	1	1	0	1	1	0	0.161 (0.152)	0.042 (0.046)	0.089 (0.087)
	1	0	1	1	0	1	0.732 (0.670)	0.328 (0.325)	0.484 (0.454)
	1	2	1	1	0	0	-3.951 (-4.076)	-3.841 (-3.989)	-4.115 (-4.233)
	1	2	0	1	0	1	-1.827 (-1.993)	-2.274 (-2.535)	-2.406 (-2.676)
	1	1	1	1	1	0	-0.779 (-0.839)	-0.885 (-0.973)	-0.943 (-1.030)
O	1	1	1	1	0	1	0.019 (-0.082)	-0.261 (-0.329)	-0.227 (-0.312)
	1	2	0	1	1	0	0.078 (0.005)	-0.195 (-0.239)	-0.130 (-0.183)
	1	2	1	1	2/3	1/3	-1.890 (-1.916)	-1.771 (-1.886)	-1.890 (-1.989)
	1	2	1	1	0	1	-1.993 (-2.176)	-2.248 (-2.433)	-2.367 (-2.555)
	1	2	1	1	1	0	-1.871 (-1.997)	-1.919 (-2.053)	-2.039 (-2.161)
	1	1	1	1	2	0	-0.760 (-0.852)	-1.060 (-0.200)	-1.107 (-1.256)
F	1	1	1	1	1	1	0.354 (0.318)	0.250 (0.234)	0.288 (0.263)
	1	2	0	1	2	0	1.307 (1.205)	0.809 (0.775)	0.976 (0.917)
	1	2	1	1	4/3	2/3	-0.471 (-0.504)	-0.463 (-0.497)	-0.491 (-0.521)
Na	1	2	1	1	2	0	-0.536 (-0.642)	-0.817 (-0.923)	-0.839 (-0.953)
	1	2	1	1	1	1	-0.471 (-0.523)	-0.523 (-0.576)	-0.549 (-0.601)
	1	0	0	0	0	0	-0.454 (-0.462)	-0.413 (-0.422)	-0.474 (-0.480)
Al	1	2/3	1/3	1	0	0	-0.260 (-0.262)	-0.253 (-0.256)	-0.297 (-0.300)
	1	0	1	1	0	0	-0.330 (-0.366)	-0.401 (-0.447)	-0.432 (-0.486)
	1	1	0	1	0	0	-0.284 (-0.296)	-0.299 (-0.317)	-0.341 (-0.360)
Si	1	4/3	2/3	1	0	0	-1.040 (-1.045)	-1.031 (-1.042)	-1.153 (-1.159)
	1	2	0	1	0	0	-1.050 (-1.095)	-1.123 (-1.180)	-1.224 (-1.284)
	1	1	1	1	0	0	-1.036 (-1.050)	-1.044 (-1.064)	-1.161 (-1.177)
	1	1	0	1	0	1	-0.418 (-0.505)	-0.541 (-0.674)	-0.590 (-0.738)
	1	1	0	1	1	0	0.108 (0.097)	0.053 (0.053)	0.075 (0.070)

P	1	0	1	1	0	1	0.494 (0.430)	0.302 (0.281)	0.381 (0.340)
	1	2	1	1	0	0	-2.389 (-2.402)	-2.384 (-2.410)	-2.601 (-2.616)
	1	2	0	1	0	1	-1.102 (-1.242)	-1.311 (-1.529)	-1.416 (-1.651)
	1	1	1	1	1	0	-0.469 (-0.506)	-0.522 (-0.581)	-0.568 (-0.630)
	1	1	1	1	0	1	0.055 (-0.014)	-0.078 (-0.127)	-0.076 (-0.139)
S	1	2	0	1	1	0	0.093 (0.044)	-0.036 (-0.061)	-0.013 (-0.048)
	1	2	1	1	2/3	1/3	-1.044 (-1.057)	-1.048 (-1.068)	-1.140 (-1.151)
	1	2	1	1	0	1	-1.120 (-1.213)	-1.251 (-1.360)	-1.352 (-1.467)
	1	2	1	1	1	0	-1.073 (-1.108)	-1.114 (-1.159)	-1.208 (-1.249)
	1	1	1	1	2	0	-0.430 (-0.519)	-0.563 (-0.692)	-0.602 (-0.743)
Cl	1	1	1	1	1	1	0.241 (0.205)	0.194 (0.174)	0.214 (0.186)
	1	2	0	1	2	0	0.898 (0.783)	0.679 (0.625)	0.766 (0.686)
	1	2	1	1	4/3	2/3	-0.263 (-0.267)	-0.265 (-0.271)	-0.286 (-0.289)
	1	2	1	1	2	0	-0.255 (-0.347)	-0.379 (-0.480)	-0.405 (-0.517)
	1	2	1	1	1	1	-0.252 (-0.277)	-0.280 (-0.307)	-0.301 (-0.329)

VWN results, with and without GGA (Becke-Perdew)

Energy changes (eV) for atoms going from restricted to (one-cycle) unrestricted. Results between parentheses are for *converged* unrestricted calculations)

All calculations have been performed in $D_{\infty h}$ symmetry, since p_x and p_y always had equal occupations and therefore could occur as π_u -x and π_u -y partners of the Π_u irrep.

El.	Occupations						VWN	VWN+Becke	VWN+Becke +Perdew
	α -spin			β -spin					
	s	p_x+p_y	p_z	s	p_x+p_y	p_z			
H	1	0	0	0	0	0	-0.868 (-0.898)	-0.758 (-0.837)	-0.889 (-0.948)
Li	1	0	0	0	0	0	-0.231 (-0.235)	-0.195 (-0.207)	-0.249 (-0.256)
Be	1	0	0	1	0	0	0.000 (0.000)	0.000 (0.000)	0.000 (0.000)
B	1	2/3	1/3	1	0	0	-0.247 (-0.255)	-0.231 (-0.242)	-0.276 (-0.281)
	1	0	1	1	0	0	-0.295 (-0.321)	-0.436 (-0.474)	-0.448 (-0.485)
C	1	1	0	1	0	0	-0.266 (-0.279)	-0.296 (-0.316)	-0.333 (-0.348)
	1	4/3	2/3	1	0	0	-1.163 (-1.203)	-1.109 (-1.158)	-1.252 (-1.285)
	1	2	0	1	0	0	-1.152 (-1.211)	-1.271 (-1.345)	-1.372 (-1.436)
	1	1	1	1	0	0	-1.152 (-1.197)	-1.134 (-1.189)	-1.267 (-1.307)
	1	1	0	1	0	1	-0.462 (-0.506)	-0.726 (-0.812)	-0.778 (-0.868)
N	1	1	0	1	1	0	0.159 (0.150)	0.039 (0.044)	0.087 (0.086)
	1	0	1	1	0	1	0.730 (0.668)	0.322 (0.319)	0.480 (0.450)
	1	2	1	1	0	0	-2.936 (-3.032)	-2.827 (-2.943)	-3.101 (-3.190)
	1	2	0	1	0	1	-1.362 (-1.454)	-1.811 (-1.972)	-1.943 (-2.108)
	1	1	1	1	1	0	-0.581 (-0.618)	-0.688 (-0.745)	-0.746 (-0.801)
O	1	1	1	1	0	1	0.178 (0.088)	-0.104 (-0.158)	-0.069 (-0.140)
	1	2	0	1	1	0	0.197 (0.135)	-0.077 (-0.109)	-0.011 (-0.053)
	1	2	1	1	2/3	1/3	-1.400 (-1.477)	-1.361 (-1.447)	-1.480 (-1.552)
	1	2	1	1	0	1	-1.442 (-1.583)	-1.698 (-1.836)	-1.816 (-1.957)
	1	2	1	1	1	0	-1.422 (-1.515)	-1.470 (-1.568)	-1.590 (-1.678)
	1	1	1	1	2	0	-0.564 (-0.623)	-0.866 (-0.960)	-0.913 (-1.013)
	1	1	1	1	1	1	0.358 (0.321)	0.255 (0.237)	0.292 (0.266)

F	1	2	0	1	2	0	1.323 (1.220)	0.825 (0.789)	0.992 (0.932)
	1	2	1	1	4/3	2/3	-0.374 (-0.398)	-0.366 (-0.391)	-0.394 (-0.416)
	1	2	1	1	2	0	-0.323 (-0.409)	-0.605 (-0.686)	-0.627 (-0.715)
Na	1	2	1	1	1	1	-0.349 (-0.389)	-0.401 (-0.441)	-0.427 (-0.467)
	1	0	0	0	0	0	-0.200 (-0.203)	-0.158 (-0.162)	-0.222 (-0.224)
Al	1	2/3	1/3	1	0	0	-0.145 (-0.146)	-0.138 (-0.140)	-0.182 (-0.183)
	1	0	1	1	0	0	-0.181 (-0.195)	-0.254 (-0.269)	-0.285 (-0.305)
Si	1	1	0	1	0	0	-0.159 (-0.164)	-0.175 (-0.182)	-0.216 (-0.224)
	1	4/3	2/3	1	0	0	-0.645 (-0.651)	-0.636 (-0.647)	-0.759 (-0.764)
	1	2	0	1	0	0	-0.625 (-0.650)	-0.700 (-0.728)	-0.801 (-0.831)
	1	1	1	1	0	0	-0.635 (-0.645)	-0.644 (-0.658)	-0.760 (-0.770)
	1	1	0	1	0	1	-0.253 (-0.288)	-0.377 (-0.437)	-0.425 (-0.495)
P	1	1	0	1	1	0	0.101 (0.090)	0.045 (0.045)	0.067 (0.063)
	1	0	1	1	0	1	0.468 (0.407)	0.275 (0.255)	0.355 (0.315)
	1	2	1	1	0	0	-1.578 (-1.592)	-1.574 (-1.598)	-1.790 (-1.805)
	1	2	0	1	0	1	-0.732 (-0.794)	-0.942 (-1.051)	-1.047 (-1.166)
	1	1	1	1	1	0	-0.313 (-0.330)	-0.366 (-0.397)	-0.412 (-0.445)
S	1	1	1	1	0	1	0.170 (0.109)	0.037 (-0.001)	0.039 (-0.012)
	1	2	0	1	1	0	0.172 (0.128)	0.043 (0.023)	0.066 (0.036)
	1	2	1	1	2/3	1/3	-0.731 (-0.743)	-0.736 (-0.753)	-0.827 (-0.837)
	1	2	1	1	0	1	-0.700 (-0.770)	-0.831 (-0.906)	-0.932 (-1.011)
	1	2	1	1	1	0	-0.729 (-0.756)	-0.770 (-0.803)	-0.864 (-0.893)
Cl	1	1	1	1	2	0	-0.282 (-0.330)	-0.415 (-0.488)	-0.454 (-0.535)
	1	1	1	1	1	1	0.239 (0.203)	0.192 (0.172)	0.212 (0.185)
	1	2	0	1	2	0	0.886 (0.773)	0.667 (0.613)	0.754 (0.675)
	1	2	1	1	4/3	2/3	-0.191 (-0.194)	-0.192 (-0.198)	-0.213 (-0.216)
	1	2	1	1	2	0	-0.100 (-0.172)	-0.225 (-0.295)	-0.251 (-0.331)
	1	2	1	1	1	1	-0.162 (-0.183)	-0.190 (-0.211)	-0.211 (-0.233)

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