Charge-Transfer Excitations Made "Simple" by Subsystem DFT

Michele Pavanello & Pablo Ramos

Department of Chemistry Rutgers University-Newark Newark, NJ

ADF Webinar Series, Feb. 24th, 2015

What is PRG interested in?

Ab-Initio Modeling of Realistically Sized Systems with subsystem DFT!

- Charge transfer phenomena
 - Electronic structure and couplings
 - Application to biosystems, and organic electrode materials
 - \rightarrow DNA, Sulfite Oxidase (SCM booth)
 - ightarrow Organic electrode materials based on croconate crystals
- Electronic structure of periodic systems [Davide Ceresoli]
 - AIMD, RT-TDDFT, Ehrenfest
 - \rightarrow RT-TDDFT, Ehrenfest (Thursday afternoon)
 - \rightarrow Ground state (Poster)
 - Application to molecules at surfaces, liquids, ionic crystals, etc
- Linear-response TD-DFT and vdW [Henk Eshuis]

Adiabatic-to-Diabatic transformation

- All-electron method
- M. Newton, R. Cave, A. Voityuk, C. Hsu, J. Subotnik, ...
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- About 20%-40% accurate [J. Chem. Phys. 140, 104105 (2014)]

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- About 20%-40% accurate [J. Chem. Phys. 140, 104105 (2014)]
- Frozen Density Embedding (FDE-ET)
 - All-electron method
 - M. Pavanello, J. Neugebauer, L. Visscher
 - New method [J. Chem. Phys. 138, 054101 (2013)]
 - Better than 10% accurate [Submitted to J. Phys. Chem. B]

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 Frozen Density Embedding (FDE): coupled Kohn–Sham equations for each subsystem

$$\frac{\delta E[\rho_I + \rho_{II}]}{\delta \rho_I} \rightarrow \left[-\frac{1}{2} \nabla^2 + v_{KS}^I(\mathbf{r}) + v_{emb}^I(\mathbf{r}) \right] \phi_i^I(\mathbf{r}) = \varepsilon_i^I \phi_i^I(\mathbf{r})$$

$$v_{\text{KS}}^{I}(\mathbf{r}) = v_{nuc}^{I}(\mathbf{r}) + \int \frac{\rho_{I}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{xc}[\rho_{I}]}{\delta \rho_{I}}$$
$$v_{emb}^{I}(\mathbf{r}) = v_{nuc}^{II}(\mathbf{r}) + \int \frac{\rho_{II}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{xc}^{nadd}[\rho_{I}, \rho_{II}]}{\delta \rho_{I}(\mathbf{r}')} + \frac{\delta T^{nadd}[\rho_{I}, \rho_{II}]}{\delta \rho_{I}(\mathbf{r}')}$$

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Non-additive functionals approximants

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- $E_{xc}^{\text{nadd}}[\rho_I, \rho_{II}]$: GGA functionals
- $T_s^{\text{nadd}}[\rho_I, \rho_{II}]$: orbital-free GGA expressions

$$\begin{aligned} v_{\text{KS}}^{I}(\mathbf{r}) &= v_{nuc}^{I}(\mathbf{r}) + \int \frac{\rho_{I}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{xc}[\rho_{I}]}{\delta \rho_{I}} \\ v_{emb}^{I}(\mathbf{r}) &= v_{nuc}^{II}(\mathbf{r}) + \int \frac{\rho_{II}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{xc}^{nadd}[\rho_{I}, \rho_{II}]}{\delta \rho_{I}(\mathbf{r}')} + \frac{\delta T^{nadd}[\rho_{I}, \rho_{II}]}{\delta \rho_{I}(\mathbf{r}')} \end{aligned}$$

Non-additive functionals approximants

E $E_{xc}^{nadd}[\rho_I, \rho_{II}]$: GGA functionals **T** $_s^{nadd}[\rho_I, \rho_{II}]$: orbital-free GGA expressions

... if use LDA:

$$\frac{\delta T^{\text{nadd}}[\rho_{I},\rho_{II}]}{\delta \rho^{I}(\mathbf{r}')} = \frac{5}{3} C_{F} \left\{ \left[\rho_{I}\left(\mathbf{r}'\right) + \rho_{II}\left(\mathbf{r}'\right) \right]^{2/3} - \left[\rho_{I}\left(\mathbf{r}'\right) \right]^{2/3} \right\}$$

Model Hamiltonian

$$\hat{H}=H_{ii}^{\prime}|i
angle\langle i|+H_{if}^{\prime}|i
angle\langle f|+H_{f\!f}^{\prime}|f
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Basis set for a hole transfer reaction

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Basis set for a hole transfer reaction

Initial state
$$\rightarrow \left[D\right]^{+} - (\text{bridge}) - \left[A\right]$$

Final state $\rightarrow \left[D\right] - (\text{bridge}) - \left[A\right]^{+}$

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The coupling

$$H_{if}^{\prime} = \langle D^{+}A|\hat{H}|DA^{+}\rangle$$

Model Hamiltonian

$$\hat{H}=H_{ii}^{\prime}|i
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Final state $\rightarrow \left[D\right] - (\text{bridge}) - \left[A\right]^{+}$

The coupling

$$H'_{if} = \langle D^+ A | \hat{H} | DA^+ \rangle$$

= $\left\langle \left[D \right]^+ - (\text{bridge}) - \left[A \right] | \hat{H} | \left[D \right] - (\text{bridge}) - \left[A \right]^+ \right\rangle$

Diabatic representation: making charge-localized states with FDE



Electronic Couplings With Subsystem DFT^a: FDE-ET

Hartree–Fock

$$H_{if} = \langle \Phi_i | \hat{H} | \Phi_f \rangle = E \left[\rho^{(if)}(\mathbf{r}) \right] S_{if}$$

where $S_{if} = \langle \Phi_i | \Phi_f \rangle$, and

$$\rho^{(if)}(\mathbf{r}) = \sum_{kl} \phi_k^{(i)}(\mathbf{r}) \left(\mathbf{S}^{(if)}\right)_{kl}^{-1} \phi_l^{(f)}(\mathbf{r})$$

where $\mathbf{S}_{kl}^{(if)} = \langle \phi_k^{(i)} | \phi_l^{(f)} \rangle$

Subsystem DFT formalism

$$H_{if} = E\left[\rho^{(if)}\right] S_{if} \qquad \dots \text{ an approximation}$$
$$H_{if} = \left[\left(\sum_{I}^{N_{S}} E\left[\rho_{I}^{(if)}(\mathbf{r})\right]\right) + T_{s}^{\text{nadd}}\left[\left\{\rho_{I}^{(if)}\right\}_{I=1,\dots,N_{S}}\right] + E_{xc}^{\text{nadd}}\left[\left\{\rho_{I}^{(if)}\right\}_{I=1,\dots,N_{S}}\right]\right] S_{if}$$
It's linear scaling!!

^a MP, Van Voorhis, Visscher, Neugebauer, JCP 138, 054101 (2013)

Hole transfer in the ethylene dimer radical cation

		Excitation Energy (eV)					
R	S_{if}	This Work ^a	CCSD(T) ^b	$CCSD(T)^{c}$	$FS\operatorname{-CCSD}^d$		
3.0	1.60E-1	1.833	1.913	1.939	1.947		
4.0	6.27E-2	0.521	0.527	0.558	0.555		
6.0	6.55E-3	0.037	0.024	0.038	0.035		
9.0	1.82E-4	6E-4	0.009	0.004	3E-4		
10.0	5.31E-5	1E-4	0.009	0.003	5E-5		
15.0	8.75E-8	2E-6	0.009	0.004	1E-7		

a PW91/TZP

- b EOM-CCSD(T)/6-311G(d,p) ROHF
- c EOM-CCSD(T)/aug-cc-pVDZ ROHF
- d FS-CCSD(T)/aug-cc-pVDZ UHF



MP, Van Voorhis, Visscher, Neugebauer, JCP 138, 054101 (2013)

The Superexchange Hole Transfer in DNA



^a Ramos and MP, JCTC 10, 2546 (2014)

Calculation of hole transfer couplings with FDE-ET

DNA base pairs: distance dependence of excitation energies and couplings^{*a*}



^a Ramos and MP, JCTC 10, 2546 (2014)

Donor-Bridge-Acceptor Effective Couplings^{*a*} with FDE-ET^{*b*}





^{*a*} A. Nitzan, Chemical Dynamics in Condensed Phases, Oxford University Press (2006) ^{*b*} Ramos and MP, JCTC **10**, 2546 (2014)

Donor-Bridge-Acceptor Effective Couplings^{*a*} with FDE-ET^{*b*}

Hole transfer in DNA oligomers:
$$\begin{array}{c}G\\C\end{array}$$
 $\begin{pmatrix}T\\A\end{pmatrix}_n$ C



^{*a*} A. Nitzan, Chemical Dynamics in Condensed Phases, Oxford University Press (2006) ^{*b*} Ramos and MP, JCTC **10**, 2546 (2014)

Donor-Bridge-Acceptor Effective Couplings^{*a*} with FDE-ET^{*b*}



Superexchange mechanism

$$V'_{DA}(E) = V_{DA} + V_{DB}G_B(E)V_{BA}$$

accounts for a lower tunnelling barrier than the vacuum: $\beta \simeq 1$

much closer to experiment^c

- ^a A. Nitzan, Chemical Dynamics in Condensed Phases, Oxford University Press (2006)
 ^b Ramos and MP, JCTC **10**, 2546 (2014)
- ^c B. Giese, Annu. Rev. Biochem. **71**, 51-70 (2002)

Effective Couplings Between Charge Separated States^a with Subsystem DFT

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Charge separation (ground state)

$$D + A \rightarrow D^+ + A^-$$

Charge separation (excited state)

 $D^* + A \rightarrow D^+ + A^-$

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HOMOs for the ethylene dimer in the charge separated state

The FDE calculation needs extra care.

The orbitals of the anions might not be correct due to self-interaction. If a selfinteraction corrected functional is used, these issues are drastically reduced.



^a Solovyeva, Pavanello, Neugebauer, JCP, 140, 164103 (2014)

Practical Calculations: outline

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Initial FDE calculations

- Compute D⁺ + A diabat A
- Compute D + A⁺ diabat B
- The input file must be prepared manually
- PyADF support is being developped (L. Vissher)

In output:

- 1 T21 file for the isolated D: t21.iso.rho1
- 1 T21 file for the isolated A: t21.iso.rho1
- 2 T21 files for the embedded D: fragA1.t21, fragB1.t21
- 2 T21 files for the embedded A: fragA2.t21, fragB2.t21

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FDE-ET calculation

Once the FDE calculations for the A and B diabats are complete, the FDE-ET calculation can follow. The keyword needed is

ElectronTransfer

Practical Calculations: Making the FDE-ET input file

Fragment key need this setup to load some predefined parameters from the isolated calculation (basis sets, AO maps, ...)

ElectronTransfer key. NumFrag specifies the number of fragments involved. InvThr is a threshold for handling quasi-orthogonality. Joint/Disjoint: the default is Joint. Disjoint is not recommended yet.

```
FRAGMENTS
rhol t21.iso.rhol
rho2 t21.iso.rho2
END
```

```
ELECTRONTRANSFER
NumFrag 2
{Joint|Disjoint}
{InvThr 1.0e-3}
END
```

See example file at:

\$ADFHOME/examples/adf/ElectronTransfer_FDE_H20

The output file from:

\$ADFHOME/examples/adf/ElectronTransfer_FDE_H20

The output file from:

\$ADFHOME/examples/adf/ElectronTransfer_FDE_H20

Is the following:

==> WARNING: one less electron in the transition density matrix <== applying the Penrose inversion of the N-1 <== ==> dimensional subspace ==> <== Some references... Electronic Coupling = 0.000000 eV Electronic Coupling = -0.000006 cm-1 H11-H22 = -1.396836 eV Excitation Energy = 1.396836 eV Overlap = 0.000000 H11 H22 H12 = -152.443044906236 -152.391712133030 -151.743951196449 Eb S11 S22 S12 = 0.981761438554 0.980941502465 -0.00000000038 Exiting Electron Transfer Program NORMAL TERMINATION END

Let's look at another output file:

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 ======
 Electron Transfer RESULTS ======

 Electronic Coupling =
 0.344469 eV

 Electronic Coupling =
 2778.314671 cm-1

 H11-H22
 =
 0.000574 eV

 Excitation Energy =
 0.688937 eV

 Overlap
 =
 0.066531

 H11 H22 H12 =
 -1384.925285303533 -1384.925306415906 -1385.114726153074 Eh

 S11 S22 S12 =
 0.880467985626
 0.880488669229 -0.058578952462

 ========
 END Electron Transfer RESULTS ==========

Let's look at another output file:

	Electron	Transfer H	RESULTS				
Electronic Co	oupling =	0.3	344469 e	eV			
Electronic Co	oupling =	2778.3	314671 d	cm-1			
H11-H22	=	0.0	000574 e	eV			
Excitation Er	nergy =	0.0	688937 e	eV			
Overlap	=	0.0	066531				
H11 H22 H12 =	-1384.925	285303533	-1384.9	925306415906	-1385.114726153074	Eh	
S11 S22 S12 =	= 0.880	467985626	0.8	380488669229	-0.058578952462		
======= H	END Electron Transfer RESULTS ====================================						

Things to note

- H11-H22 is the energy difference of the diabatic states
- Excitation Energy may differ from H11-H22

 Overlap is the normalized overlap

$$S_{ij}' = rac{S_{ij}}{\sqrt{S_{ii} imes S_{jj}}}$$

FDE-ET in summary

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- Tested for hole transfer.

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- Applied to hole transfer and charge separation in pilot calculations.
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Recommendations

- Use the PW91k nonadditive Kinetic Energy functional in the FDE calculations.
- No particular problems applying FDE-ET to cations (hole transfer) → InvThr: might need 1.0e-2 if a near orthogonality is suspected.
- Application to anions is not recommended, however it is possible. Use SIC functionals in the FDE part, and then a GGA functional in the ElectronTransfer part.
- Application to charge separation (+/-) and to other spin states (e.g. triplet) is not available in the released code. Perhaps in the next ADF release.

I am looking for...

PhD & Master's students

Available Projects

. . . .

- Non-adiabatic dynamics with Subsystem DFT
- Van der Waals interactions between subsystems
- Subsystem DFT applied to Materials research

Rutgers University, Newark, NJ

- 20' from NYC
- Fun learning environment

Acknowledgments

Postdocs, Students & Collaborators

- Dr. Debalina Sinha
- Pablo Ramos
- Marc Mankarious

- Prof. J. Neugebauer (WWU, Münster)
- Prof. L. Visscher (VU, Amsterdam)
- Prof. T. Van Voorhis (MIT)

Funding

- Start-up funds from Rutgers-Newark
- NSF-CBET-1438493
- NSF-CNIC-1404739

- AMSTERDAM DENSITY FUNCTIONAL
- Petroleum Research Fund (54063-DNI6)
- ELF fund State of New Jersey